

HW #4

7.2

$$\left. \frac{dN_2}{dt} \right|_{\text{stim}} = B_{21}N_2\rho(\nu) = \frac{(c')^3}{8\pi h\nu^3} A_{21}N_2\rho(\nu); \quad \left. \frac{dN_2}{dt} \right|_{\text{spont}} = -A_{21}N_2$$

But $\rho(\nu) = \frac{8\pi h\nu^3}{(c')^3} N_p$, where N_p = photons per mode; $\therefore \frac{\text{stimulated rate}}{\text{spontaneous rate}} = N_p$

7.3

$$\int_0^{\infty} g(\nu) d\nu = 1 = K \cdot (2.667 \text{ cm}^{-1}) \text{ or one could convert to frequency units;}$$

$$\therefore K \cdot (8 \times 10^{10} \text{ Hz}) = 1; K = 1.25 \times 10^{-11} \text{ sec} = g(\nu_0); \bar{\nu}_0 = 15,713 \text{ cm}^{-1}; \lambda_0 = 0.6364 \mu\text{m}$$

$$\sigma_{\text{SE}} = \frac{\lambda^2}{8\pi} A_{21}g(\nu_0) = 2.01 \times 10^{-20} \text{ cm}^2; \quad g_2 = 3, g_1 = 5, \sigma_{\text{abs}} = 1.21 \times 10^{-20} \text{ cm}^2$$

7.5

The intent of this problem is to introduce some of the numerical factors associated with optical transitions. Given information: $\lambda_0 = 5000 \text{ \AA}$ and a wave length interval of $\Delta\lambda = 1 \text{ \AA}$, $V = 2 \text{ cm}^3$. While λ is one of the easiest parameters to measure, frequency ν is a better theoretical variable. $\therefore \nu_0 = 600 \text{ THz}$. We convert the wavelength interval into a frequency

one by: $\frac{\Delta\nu}{\nu} = \frac{\Delta\lambda}{\lambda}$ or $\Delta\nu = 1.2 \times 10^{11} \text{ Hz}$ or $\Delta\nu = 120 \text{ GHz}$ or $\Delta\bar{\nu} = 4 \text{ cm}^{-1}$ (a)

There seems to be a "natural" tendency for the student to make the following mistake once, so let me make it for you in hopes that you will NOT do the following:

$$\Delta\nu = \frac{c}{\Delta\lambda} \quad \text{which is absolutely wrong}$$

(Check the numbers: If the above were correct, then $\Delta\nu = 3 \times 10^{18} \text{ Hz}$ which is far greater than the central frequency of 600 THz.)

The number of modes in the volume V is: $N = [8\pi\nu^2\Delta\nu/c^3] V = 8.04 \times 10^{10}$ modes which is the total number of ways that electromagnetic energy can appear in that wavelength interval. Now lets look at the spectral issue on a frequency scale with zero suppressed (or in the next county). The FSR = $c/2d = 750 \text{ MHz}$