

HW #3

6.11

$$\tau_p = \frac{3/c}{1 - T_2 R_1 R_2 R_3} = 78.7 \text{ ns};$$

$$\therefore \Delta\omega_{1/2} = 1/\tau_p = 12.7 \times 10^6 \text{ r/s}; \omega_0 = 2.98 \times 10^{15} \text{ r/sec}; Q = 2.43 \times 10^8$$

6.20

$$\text{Round-trip time} = 5 \text{ nsec} = \frac{2d}{c}; \therefore d = 75 \text{ cm}; \nu_0 = 5.37 \times 10^{14} \text{ Hz}$$

$$\text{Using the slope at } t = 0, \tau_p = 75 \text{ nsec (by extrapolating)} = \frac{2d/c}{1 - R_1 R_2}; \therefore R_1 R_2 = 0.933$$

$$\Delta\nu_{1/2} = \frac{1}{2\pi\tau_p} = 2.12 \times 10^6 \text{ Hz}; \therefore Q_0 = 2.53 \times 10^8 \text{ and } F = \frac{c/2d}{\Delta\nu_{1/2}} = \frac{200 \times 10^6}{2.12 \times 10^6} = 94.2$$

$$\text{With pumping, the photon lifetime increases to: } \tau_p = 125 \text{ nsec} = \frac{2d/c}{1 - G^2 R_1 R_2}$$

$$\therefore G^2 R_1 R_2 = 0.960; \text{ Using the value of } R_1 R_2 \text{ found above leads to: } G^2 = 1.0286 \text{ or } G = 1.0142 = \exp[\gamma_0 l_g]; \therefore \gamma_0 = 1.878 \times 10^{-4} \text{ cm}^{-1}$$

6.29

$$(a) \text{ At A, } (\omega/c)n_1 d = q\pi; \text{ at B } (\omega/c)n_2 d = (q+1)\pi; \text{ subtract: } n_2 - n_1 = \lambda_0/2d = 3.16 \times 10^{-5}.$$

$$(b) \text{ The FSR} = c/2d = 30 \text{ GHz which corresponds to the spacing between the peaks of 32 divisions; The FWHM is } \sim 2.2 \text{ divisions;}$$

$$\text{Thus } F = 32/2.2 = 14.5. \Delta\nu_{1/2} = 30 \text{ GHz} + F = 2.06 \text{ GHz}; \nu = 4.74 \times 10^{14} \text{ Hz};$$

$$Q = \nu/\Delta\nu_{1/2} = 2.3 \times 10^5.$$